

A New Tip Correction Based on the Decambering Approach

Jens N. Sørensen Kaya O. Dag Néstor Ramos-García



DTU Wind Energy Department of Wind Energy



Overview

- Introduction
- The approach
- Implementation
- Comparisons with BEM and LLT applications.



Introduction

- BEM, LLT → blade is not a surface but a line
- Angle of attack represented at 1/4-chord point



- Inductions at trailing edge > leading edge
- Downwash induced by the free vortices causes curved streamlines along the chord



Induction from the wake





Decambering

- In the tip region, the flow is pushed downwards at the trailing edge as a result of strong vortex induction from the tip vortex
- Effect of the curved streamlines can be modeled by transfering their curvature to the airfoil section





The correction



Biot-Savart Law

$$q = \frac{\Gamma}{4\pi} \frac{(r_1 + r_2)(\vec{r_1} \times \vec{r_2})}{r_1 r_2 (r_1 r_2 + \vec{r_1} \cdot \vec{r_2})}$$
$$w_{jk} = \sum_{i=1}^{N} a_{ijk} \Gamma_i, \quad u_{jk} = \sum_{i=1}^{N} b_{ijk} \Gamma_i$$

Induced Cambering

$$\left. \frac{d\eta}{dx} \right|_{jk} = \frac{w_{jk} - w_{j,c/4}}{||V_{rel,j}||\cos\alpha_j + u_{jk} - u_{j,c/4}|}$$

Thin airfoil theory

$$\alpha_{L0} = -\frac{1}{\pi} \int_0^\pi \frac{d\eta_c}{dx} (\cos\theta - 1)d\theta$$

$$C_l = 2\pi(\alpha - \alpha_{L0})$$

$$\Delta C_{l,j} = 2\Delta\theta \sum_{k=1}^{M} \frac{(w_{jk} - w_{j,c/4})(\cos\theta_k - 1)}{V_{rel,j}\cos\alpha_j + (u_{jk} - u_{j,c/4})}$$



The correction

Kutta-Joukowsky theorem is employed to correct the circulation directly.

$$\Gamma = \frac{1}{2}cV_{rel}C_l \qquad \qquad \Delta C_{l,j} = 2\Delta\theta \sum_{k=1}^M \frac{(w_{jk} - w_{j,c/4})(\cos\theta_k - 1)}{V_{rel,j}\cos\alpha_j + (u_{jk} - u_{j,c/4})}$$

$$\Delta\Gamma_j = \frac{\Delta\theta \cdot c_j}{\cos\alpha_j} \sum_{k=1}^M (w_{jk} - w_{j,C/2})(\cos\theta - 1).$$



Lifting line – planar wing



Optimum rotor blades



$$\lambda = 6$$
$$AoA = 1.7^{\circ}$$

 $C_{1} = 0.7$

$$a_{opt} = 1/3 \quad a'_{opt} = \frac{2}{9\lambda^2 y^2}$$

$$\beta = \tan^{-1} \left(\frac{1-a}{\lambda y(1+a')} \right)$$

$$N_b C_l\left(\frac{c}{R}\right) = \frac{8\pi\cos\phi a'}{1+a'}y$$





1-Bladed Rotor





2-Bladed Rotor



11 **DTU Wind Energy, Technical University of Denmark**



3-Bladed Rotor





Wake length dependency





NREL 5MW Rotor @8m/s





Conclusions & future work

- Decambering effect is stronger on trapezoidal shaped blades. ~10% circulation change on a 3-bladed optimum rotor
- For NREL 5MW rotor, it is found that the new correction only has little influence on performance (~1%) and relatively high influence on thrust (~7%)
- AL implementation
- More efficient model with respect to numerical implementation.